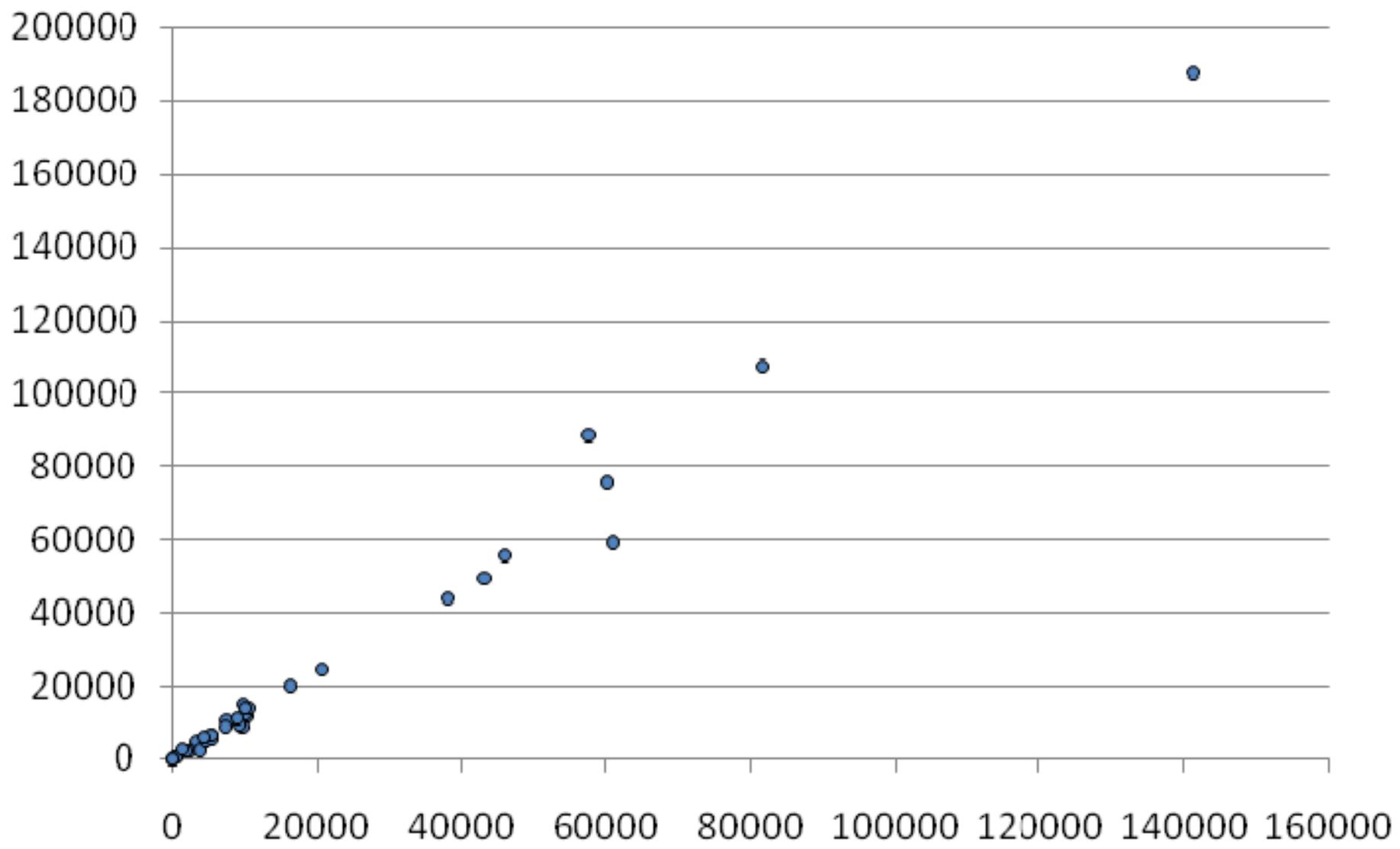


# WATCH YOUR MIND! IT'S STATISTICS

WITH FOLLOWING REVEAL



# WHAT IS STATISTICS?

THAT'S AN ART TO MAKE REASONABLE  
CONCLUSIONS USING SMALL SAMPLES  
OF DATA

Y.TYURIN

## WHAT IS STATISTICAL DATA?

ANYTHING YOU USE FOR EXTRACTING  
INFORMATION FROM

**PICTURING IS  
A GREAT  
DEAL EXITING  
OCCUPATION,**

**IF ONLY YOU  
LIKE PENCILS.  
EVEN IF YOU  
DON'T KNOW  
GEOMETRY**





**BUT IF YOU  
LEARN A BIT  
MORE THAN  
JUST USING  
PENCILS...**

**5**

**FOR EXAMPLE  
ABOUT  
PERSPECTIVE  
OR SCALAR  
PRODUCT**

# LET'S CHECK YOUR IQ

6

Q1

ROBIN ↔ BOBIN

HUMPTY ↔ ?????

# CONTINUE

Q2

**STATISTICS**  $\longleftrightarrow$  **PROB. THEORY**

**??????????**  $\longleftrightarrow$  **GEOMETRY**

# HOW DOES IT WORK?

**COMPARE DETERMINISTIC AND  
PROBABILISTIC WAYS**

# DETERMINISTIC WAY OF THINKING

9

GIVEN THAT  $0 < 1$  (TRUE),  
PROVE:  $1 < 2$ .

FROM THE OTHER:

ASSUME (HYPOTHESIS) THAT  $1 \geq 2$ .

IF SO THEN SUBTRACT 1 FROM BOTH PARTS:

$$0 \geq 1.$$

THAT'S IMPOSSIBLE. CONTRADICTION.

THE ASSUMPTION IS REJECTED FOR SURE

**STATISTICS IS LIFE.  
LIFE IS NOT MUCH DETERMINISTIC**

# BRITISH SCIENTISTS HAVE JUST DISCOVERED

EVERYTHING IS  
POSSIBLE BUT  
A SIGNIFICANT  
PART OF  
EVERYTHING  
IS UNBELIEVABLE





# PROBABILISTIC WAY OF THINKING

13

GIVEN: LIKELY EVENTS HAVE  $Pr \geq 0,05$  (MAY BE TRUE)

CHECK THE HYPOTESIS:

AT LEAST HALF OF CANDIES IN THE 2<sup>ND</sup> BAG ARE GREEN

IF SO THEN

$$Pr(\text{PURPLE}) < ???$$

FROM THE SAMPLE:

$$Pr(5 \text{ PURPLE IN ROW}) < ???$$

THAT'S UNLIKELY!

THE HYPOTHESIS'S REJECTED PRACTICALLY FOR SURE (ON THE CHOSEN LEVEL).

# PROBABILISTIC WAY OF THINKING

14

GIVEN: LIKELY EVENTS HAVE  $Pr \geq 0,05$  (MAY BE TRUE)

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# PROBABILISTIC WAY OF THINKING

15

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CHECK THE HYPOTESIS:

AT LEAST HALF OF CANDIES IN THE 2<sup>ND</sup> BAG ARE GREEN

IF SO THEN

$$\Pr(\text{PURPLE}) < 0.5$$

FROM THE SAMPLE:

$$\Pr(5 \text{ PURPLE IN ROW}) < 0.5^5 = 1/32 < 0.05$$

THAT'S UNLIKELY!

THE HYPOTHESIS'S REJECTED PRACTICALLY FOR SURE (ON THE CHOSEN LEVEL).

# LET'S COMPARE

16

DETERMINISTIC	PROBABILISTIC
AN ASSUMPTION	A HYPOTHESIS
LOOKING FOR A CONTRADICTION WITH THE ASSUMPTION	LOOKING FOR A UNLIKELY EVENT WITH THE HYPOTHESIS
IF FOUND: THE ASSUMPTION IS WRONG FOR SURE	IF : THE HYPOTHESIS REJECTED ON THE CHOSEN LEVEL (AFFORDABLE PROBABILITY)
IF NOT FOUND: ??????????	IF NOT: ??????????

# LET'S COMPARE

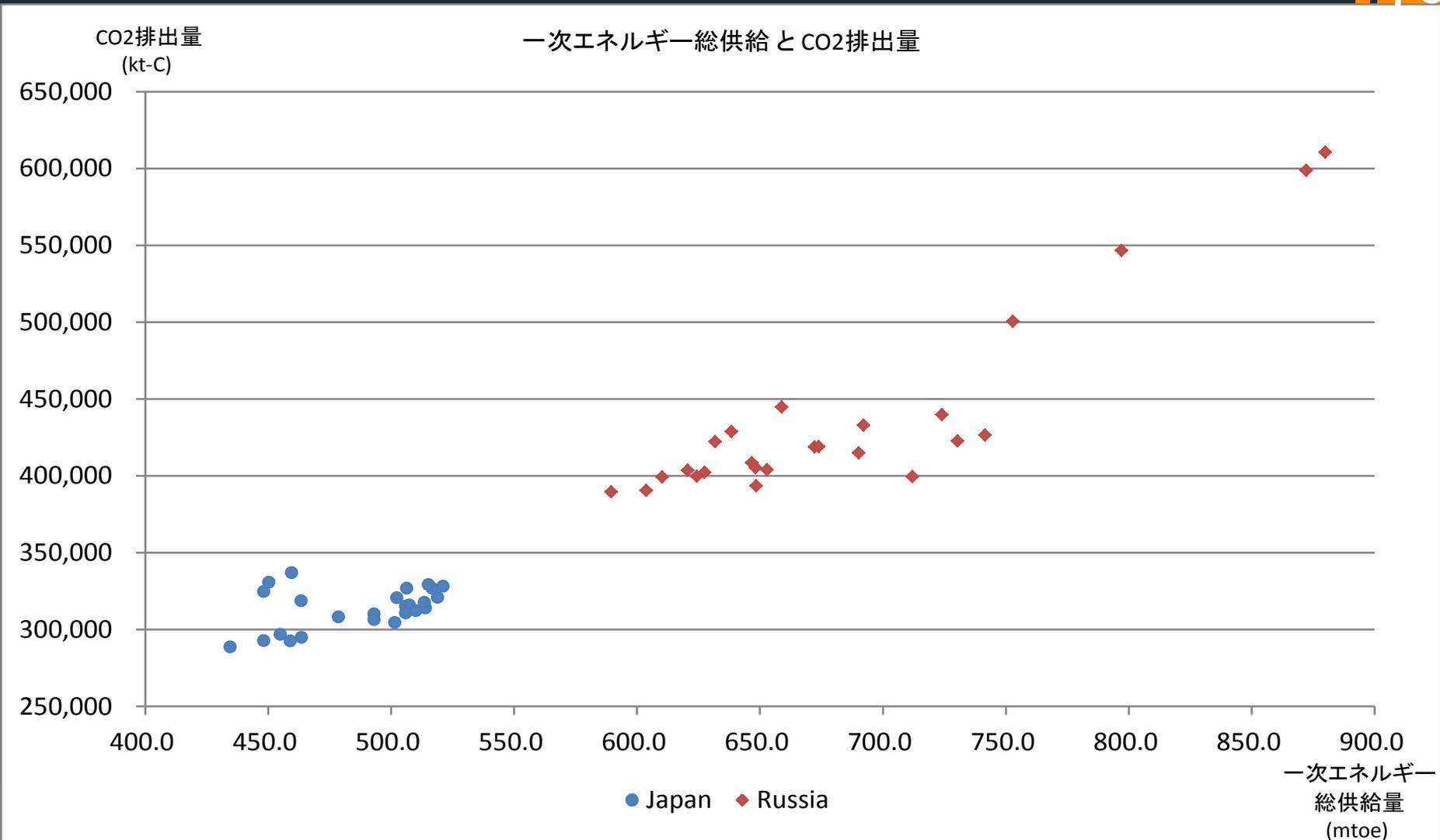
17

DETERMINISTIC	PROBABILISTIC
AN ASSUMPTION	A HYPOTHESIS
LOOKING FOR A CONTRADICTION WITH THE ASSUMPTION	LOOKING FOR A UNLIKELY EVENT WITH THE HYPOTHESIS
IF FOUND: THE ASSUMPTION IS WRONG FOR SURE	IF : THE HYPOTHESIS REJECTED ON THE CHOSEN LEVEL (AFFORDABLE PROBABILITY)
IF NOT: <b>THE ASSUMPTION CAN'T BE REJECTED (DOESN'T MEEN IT'S TRUTH)</b>	IF NOT: ??????????

# LET'S COMPARE

18

DETERMINISTIC	PROBABILISTIC
AN ASSUMPTION	A HYPOTHESIS
LOOKING FOR A CONTRADICTION WITH THE ASSUMPTION	LOOKING FOR A UNLIKELY EVENT WITH THE HYPOTHESIS
IF FOUND: THE ASSUMPTION IS WRONG FOR SURE	IF : THE HYPOTHESIS REJECTED ON THE CHOSEN LEVEL (AFFORDABLE PROBABILITY)
<b>IF NOT: THE ASSUMPTION CAN'T BE REJECTED</b>	<b>IF NOT: THE HYPOTHESIS CAN'T BE REJECTED ON THE CHOSEN LEVEL</b>



$$\hat{R} = 0,8$$

# PROBABILISTIC WAY OF THINKING

20

GIVEN: LIKELY EVENTS HAVE  $\Pr \geq 0,05$

CHECK THE HYPOTESIS:

ENERGY SUPPLY AND CO<sub>2</sub> EMISSION ARE  
INDEPENDENT VALUES

IF SO THEN  $R = 0$

FROM THE SAMPLE:  $\hat{R}=0,8$

$$\Pr(|\hat{R}| \geq 0,8) < 0,05$$

THE HYPOTHESIS'S REJECTED

# TYPES OF STATISTICS

21

**DATA REPRESENTATION**

**DESCRIPTIVE STATISTICS**

**MATH STATISTICS (VERIFICATION,  
MODELLING) – NEEDS PROB.THEORY**

**JUST SO STATISTICS (AS A SORT OF  
ENTERTAINMENT)**

# TYPES OF STATISTICS

22

DATA REPRESENTATION

DESCRIPTIVE STATISTICS

SEARCHING AND POSING HYPOTHESES

DO NOT MIX,  
PLEASE

**MATH STATISTICS USING PT  
(VERIFICATION, MODELLING)**

**JUST SO “STATISTICS” (AS AN  
ENTERTAINMENT OR CHEATING)**

## MAKING HYPOTHESES

INTERESTING, EXITING, EDUCATIONAL,  
DEVELOPING

## VERIFYING HYPOTHESES

IMPOSSIBLE UNTIL WE USE PR.THEORY

MAKING CONCLUSIONS FOR SURE  
HARMFUL, DISTRACTING, CREATING  
FALSE IMAGINATIONS

## SO, LET US:

- ENJOY STATISTICS WITHOUN PRETENDING WE APPLY 'A SCIENTIFIC METHODS'
- KEEP AND DEVELOP CRITICAL REASONING
- UNDERSTAND THE NATURAL BOUNDARIES OF OUR RESEARCHS WITH STUDENTS
- LEARN ABOUT PROBABILITIES TO EXPAND OUR CAPABILITIES IN INVESTIGATING THE WORLD

**THANK YOU, FRIENDS**

**SCHOOL PROBABILITY LAB:**  
**<http://ptlab.mccme.ru>**